## Discrete Geometry I

## Homework \# 6 - due ??

Two weeks time for this sheet. Please mark three problems that will be graded.

Exercise 1. i) What is the diameter of the permutahedron $\Pi_{d-1}=\Pi(1,2, \ldots, d)$ ?
ii) What is the diameter of a zonotope $Z=\sum_{i=1}^{k}\left[-z_{i}, z_{i}\right]$ ?
iii) True or false: If $P$ is centrally-symmetric, then $\operatorname{diam}(P)=\operatorname{dist}(u,-u)$ for some $u \in V(P)$.

Exercise 2. Let $P \subset \mathbb{R}^{3}$ be a three dimensional polytope.
i) What is the f -vector of the truncation of $P$ at a vertex $v$ ?
ii) What is the operation polar to truncating a vertex?
iii) Let

$$
\mathcal{F}_{3}=\left\{\left(f_{0}, f_{1}, f_{2}\right) \mathbb{Z}^{3}: f_{0}-f_{1}+f_{2}=2, f_{0} \leq 2 f_{2}-4, f_{2} \leq 2 f_{0}-4\right\}
$$

Show that every $f \in \mathcal{F}_{3}$ is the f -vector of a 3 -polytope.

