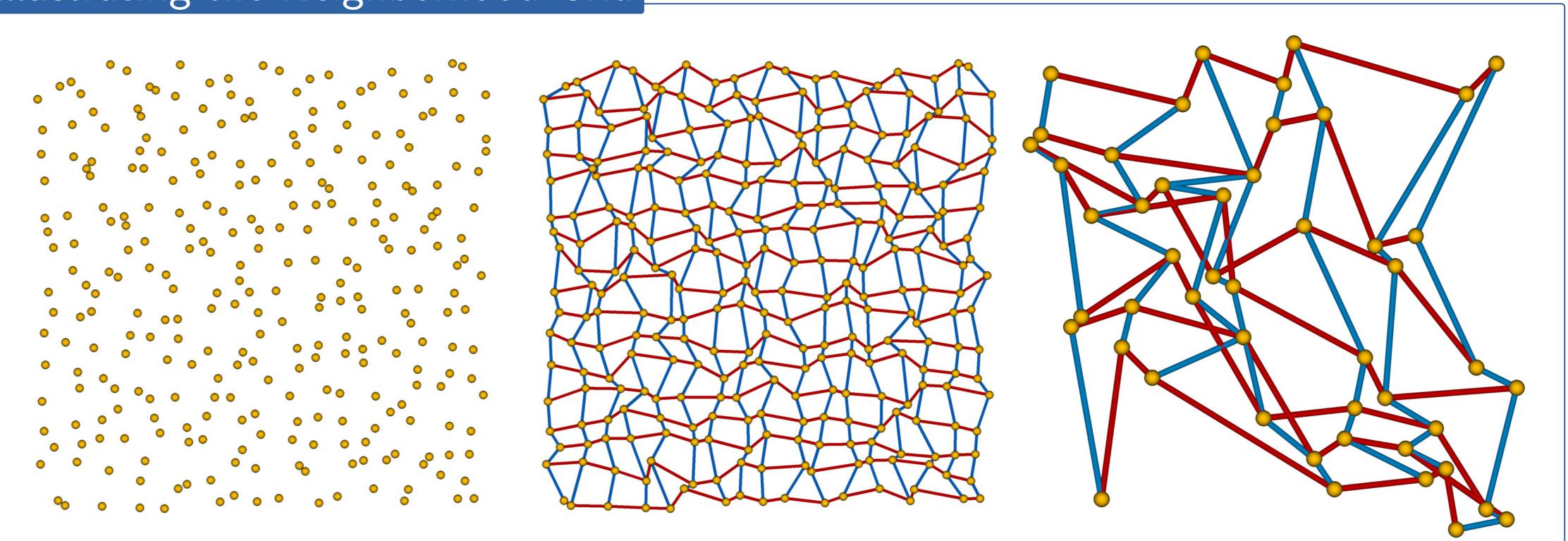


Computational and Structural Aspects of Point Set Surfaces

The Neighborhood Grid

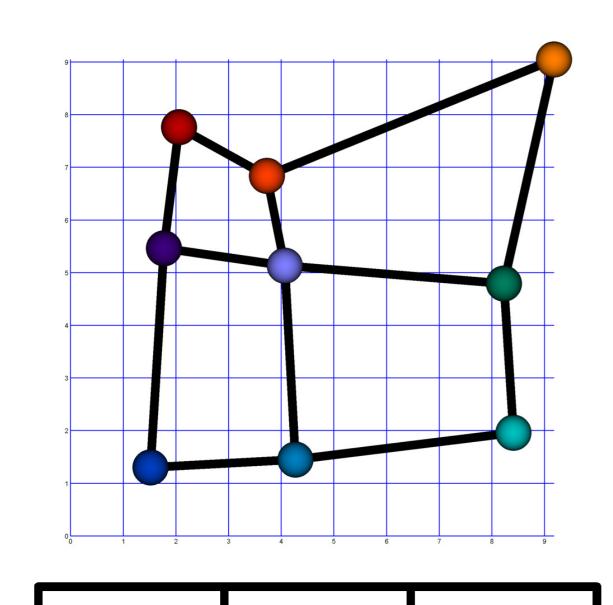
The Neighborhood Grid approximates neighborhood information. A (quadratic) matrix contains the coordinates of the points such that in each row the x-values are increasing while in each column the y-values are increasing. For the algorithm, the order of the points suffices, the exact coordinates are irrelevant. If the above ordering is given, we call it a "stable state".

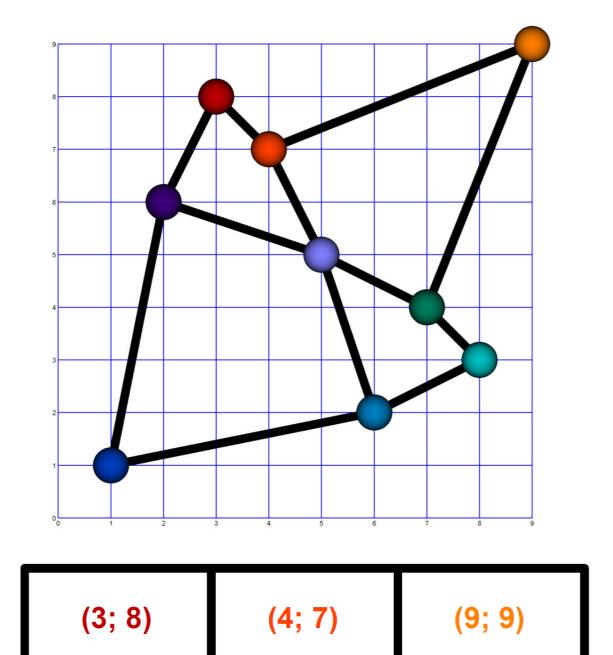
Illustrating the Neighborhood Grid



From left to right: A raw point cloud, the corresponding structure induced by the grid, and an example where the neighborhood is not faithfully recovered.

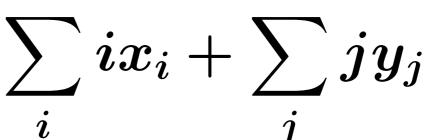
Order Preservence



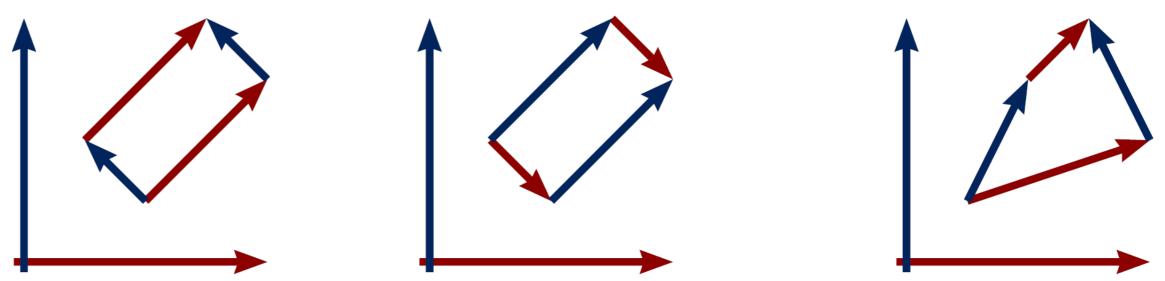


Energy / Uniqueness of Stable States

Summing x-values with column-numbers and y-values with rownumbers, the resulting energy grows when exchanging wrongly sorted pairs.



However, the resulting stable states do not have to be unique.

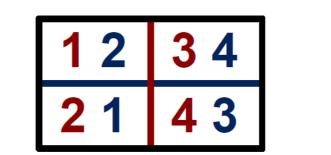


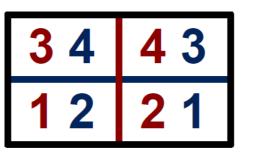
(1,77; 5,46)	(4,07; 5,13)	(8,23; 4,79)
(1,53; 1,30)	(4,27; 1,45)	(8,41; 1,96)

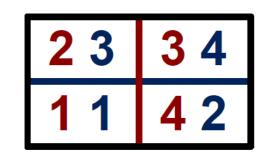
(2,06; 7,76) (3,73; 6,84) (9,18; 9,05)

(2; 6)	(5; 5)	(7; 4)
(1; 1)	(6; 2)	(8; 3)

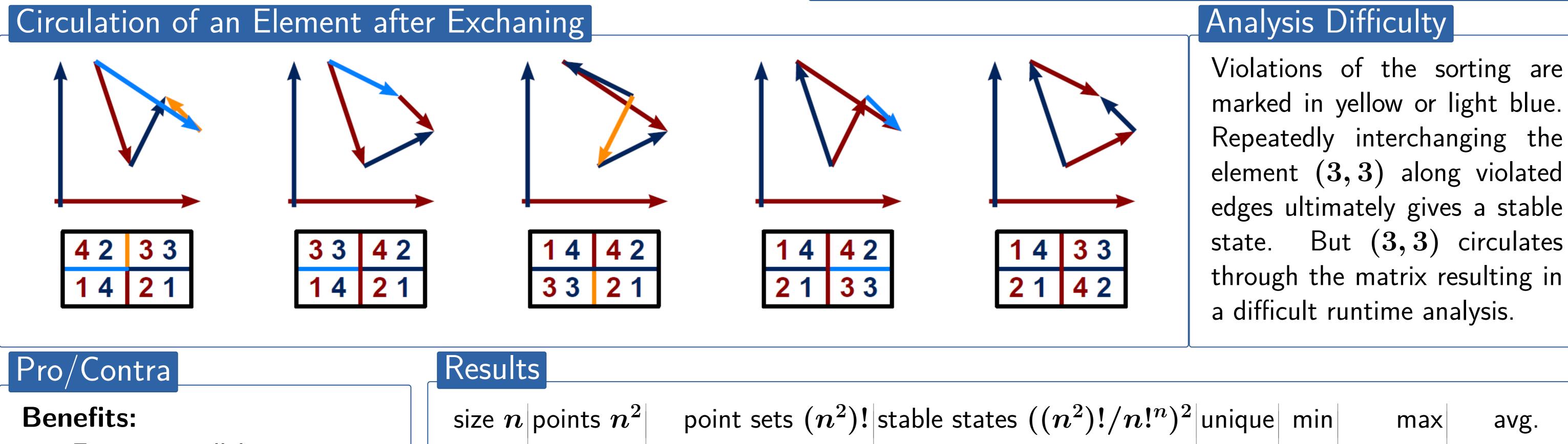
Reducing from rational to integer values keeping the order.







Two different stable states for one point configuration and a 2 imes 2 configuration with a unique stable state.



Easy to parallelize.	1	1	1	1	1	1	1	1.0
Const. time approximation.	2	4	24	36	12	1	2	1.5
Disadvantages:	3	9	362,880	2,822,400	966	1	42	7.777
 No lower-dim. points. Approx. might be bad. 	4	16	20,922,789,888,000	3,976,941,969,000,000	0	$\leq 8 \geq 2$	24,024	90.077
Applications	Re	ference	S					
 Crowd Simulation [1]. Fluid Animation [2]. Biological Cell Simulation [3]. 	[2	GPU", 2009 [] M. Joselli, M. J	9. J. R. da S. Junior, E. W. Clua, A. Monte computing", 2015.	ontenegro, and B. Feijó. "A Neighborhood Grid enegro, M. Lage, and P. Pagliosa. "Neighborhoo ple and Efficient Approximate Nearest Neighbor	od grid: A no	ovel data str	ucture for flui	

Corresponding Author: Martin Skrodzki, Workgroup Geometry Processing, FU Berlin, Germany, martin.skrodzki@fu-berlin.de