



# PAKT FOR RESEARCH AND INNOVATION: THE RESEARCH NETWORK COUPLED FLOW PROCESSES IN ENERGY AND ENVIRONMENTAL RESEARCH

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## Coupled Flow Processes — an Interdisciplinary Problem

**Appearance of coupled flow processes:** energy research, geo sciences, environmental and climate research, civil engineering, materials science

### Research topics of the network:

- ▷ reactive transport of dissolved species
- ▷ interaction between free flow and flow in porous media
- ▷ exchange processes in multi-phase flows

### Mathematical models:

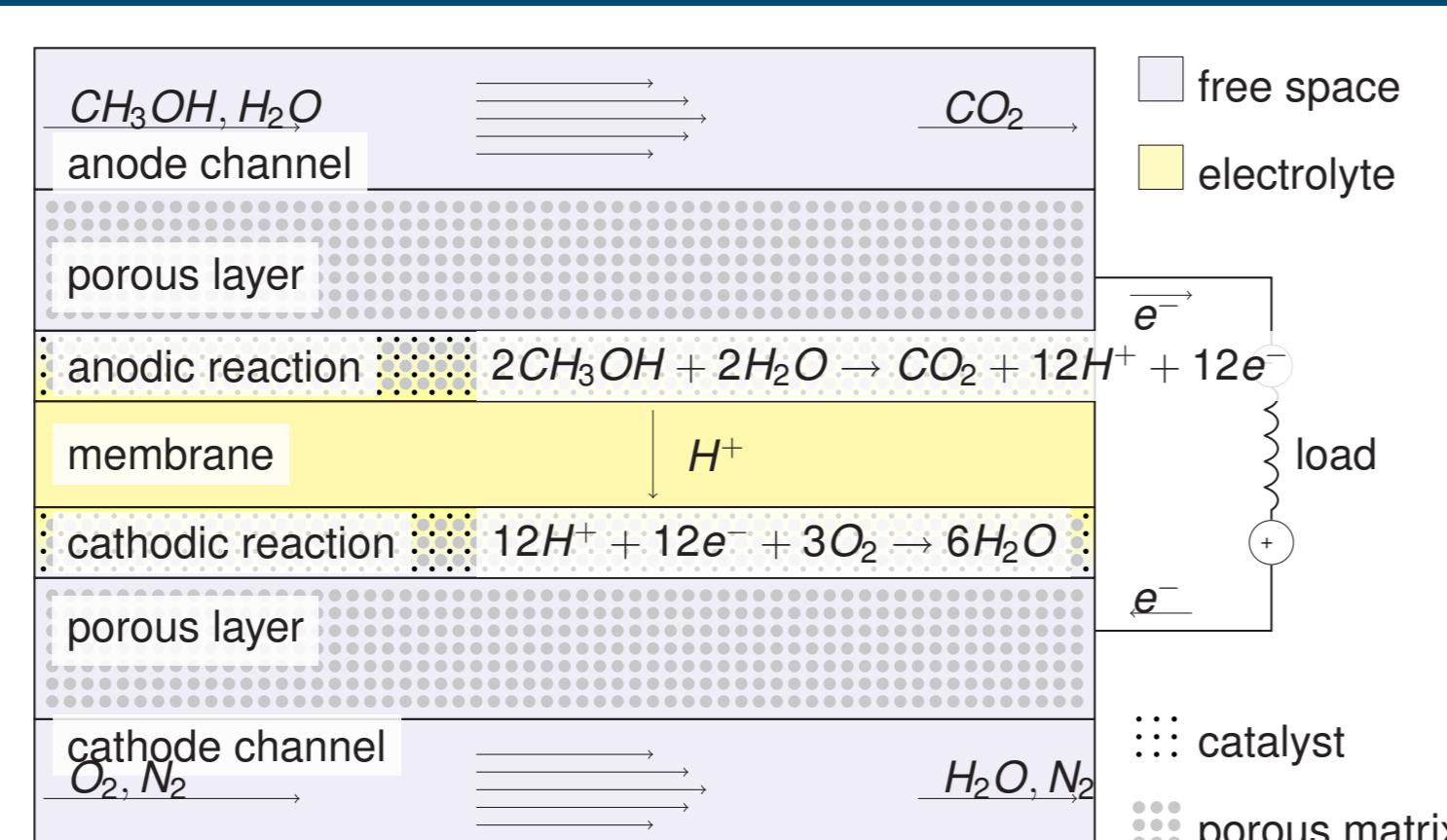
- ▷ free flow: (incompressible) Navier-Stokes equation
- ▷ porous media flow: Darcy and Brinkman model
- ▷ soil hydrology: (stochastic) Richards equation
- ▷ species transport: reaction-diffusion-convection equation
- ▷ interface conditions: boundary layer theory, Beavers-Joseph, ...

## The Projects

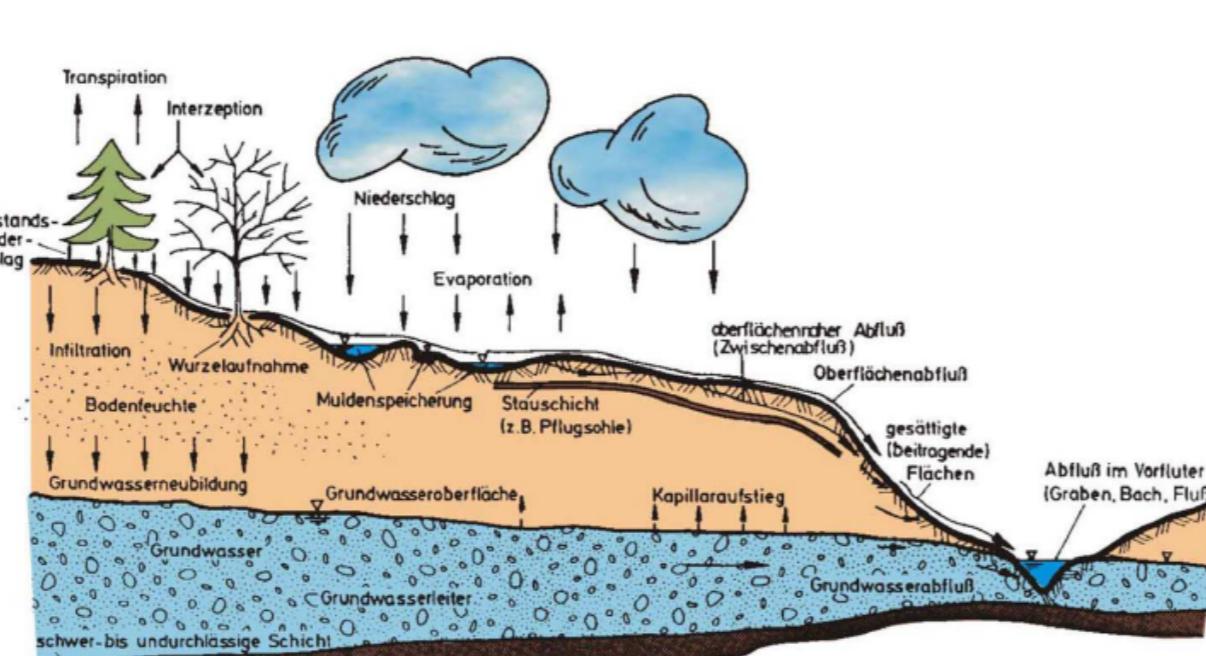
- ▷ **WIAS-I:** discretization of incompressible Navier-Stokes equation by covolume methods preserving the discrete maximum principle in coupled reaction-convection-diffusion equations
- ▷ **WIAS-II:** appropriate interface conditions for the coupling of free flow and porous media flow, two and three-layer models, and numerical implementation
- ▷ **PIK-I:** coupling of dynamic climate model CLM with the soil model TERRA-ML, horizontal water transport in soil and groundwater
- ▷ **FU-I:** simulation of the stochastic Richards equation for water flow in homogeneous soil and coupling with atmosphere processes, systematic uncertainty analysis using polynomial chaos expansion
- ▷ **FU-II:** Analysis of Ekman boundary layer for variations in the vegetation height and derivation of new boundary conditions for atmosphere-land-surface interaction, systematic uncertainty analysis using polynomial chaos expansion
- ▷ **FAU-I:** efficient simulation of multi-phase flow with Marangoni convection at the free surface between liquid and gas

## Main Applications

- ▷ **fuel cells:**
  - ▷ electrochemistry in WIAS-I and WIAS-II
  - ▷ bubble transport in FAU-I



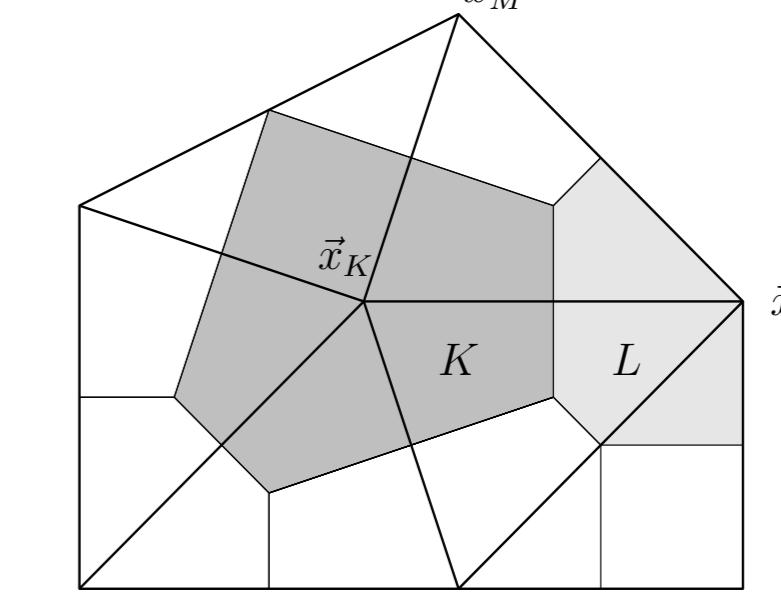
- ▷ **regional climate modelling**
  - ▷ flood protection in PIK-I and FU-I
  - ▷ flow simulation of the atmosphere in FU-II



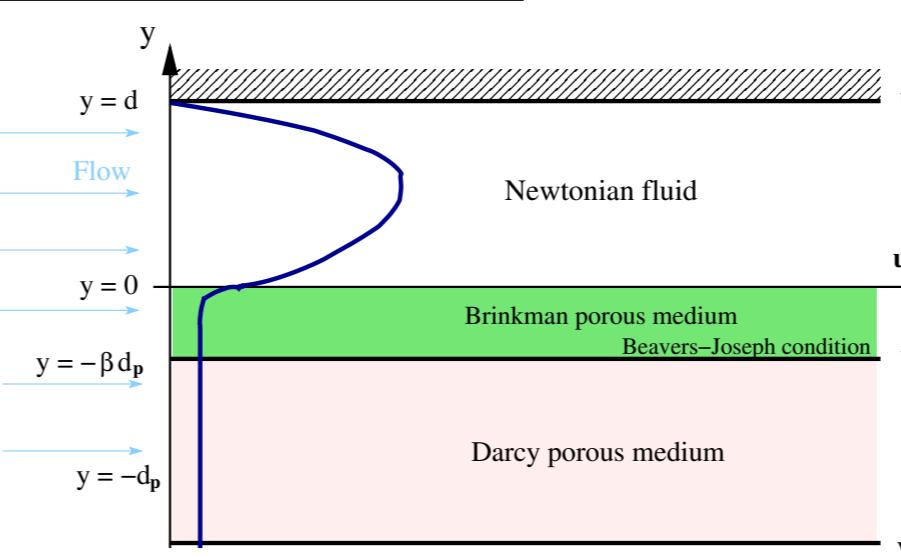
## State of the Work

### Project WIAS-I:

Taylor-Hood finite element discretization yields to a violation of the discrete maximum principle for a coupled convection-diffusion eq.



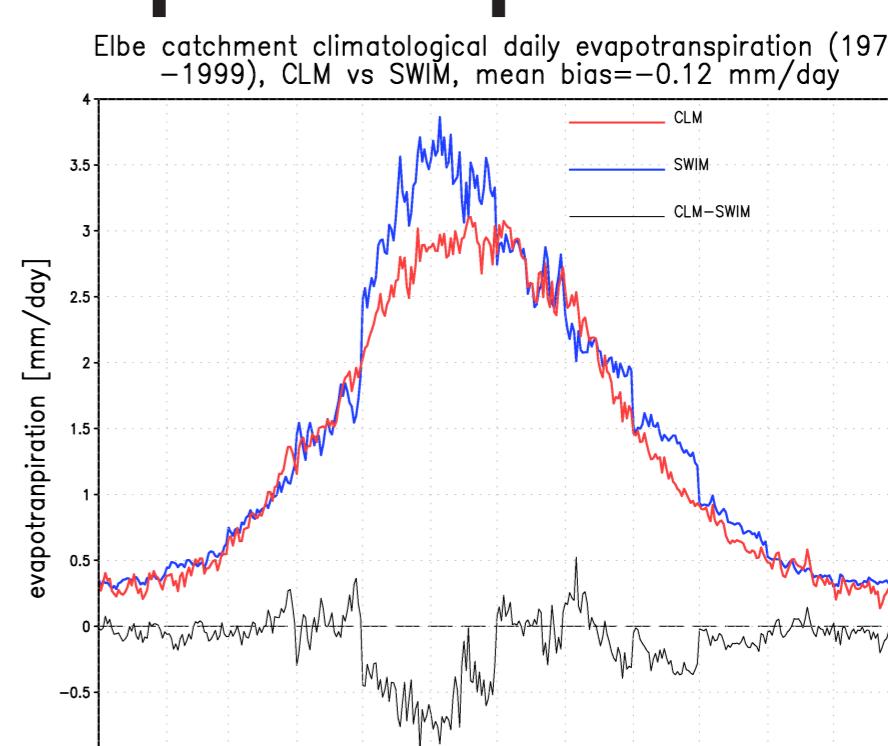
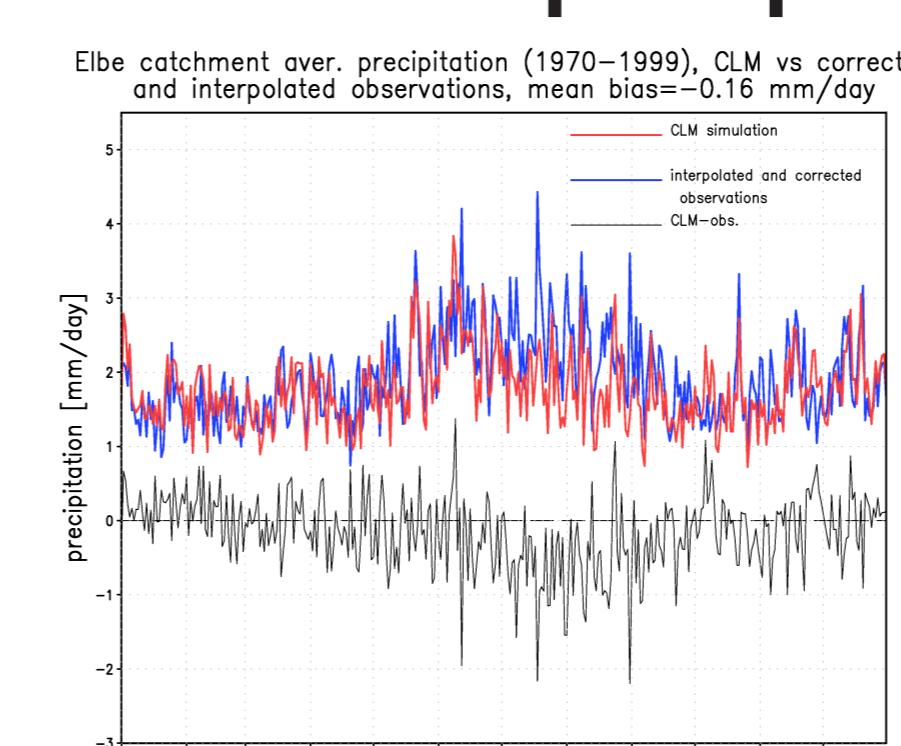
### Project WIAS-II:



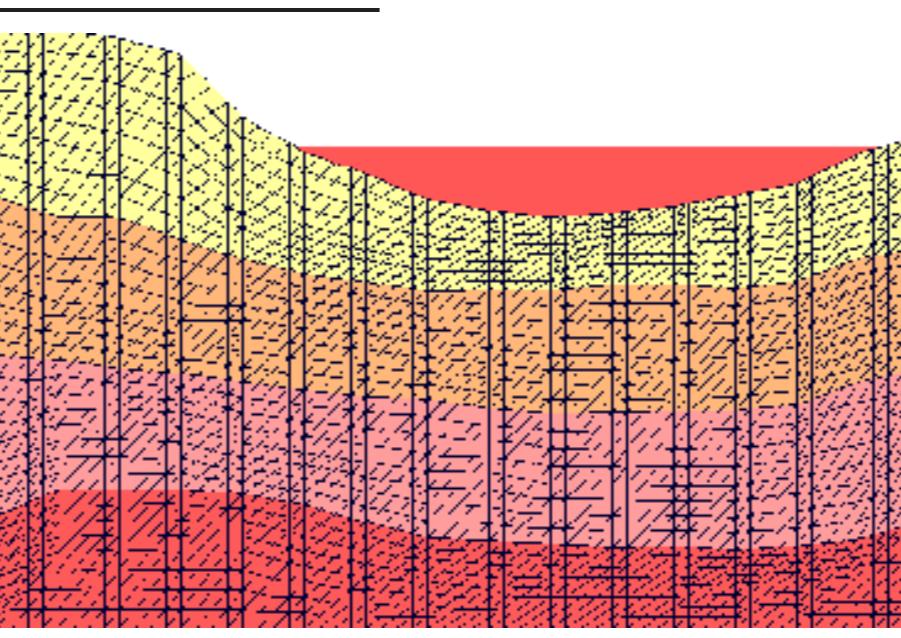
Three-layer model using a Brinkman model to resolve properly the boundary layer structure at the fluid-porous interface

### Project PIK-I:

Elbe catchment: CLM and measured data.  
Good results for **precipitation** and **evapotranspiration**.



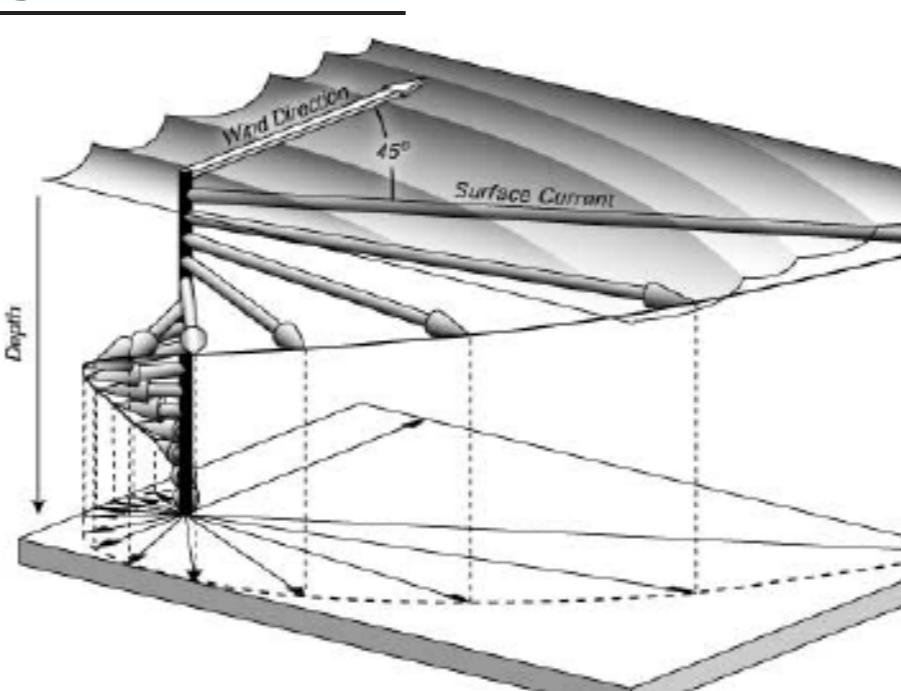
### Project FU-I:



Numerical modelling for seepage of a lake:

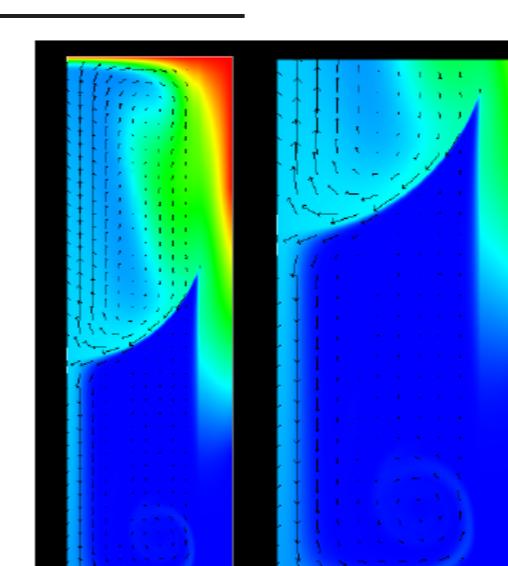
Layers in the ground: sand, loamy sand, sandy loam, loam

### Project FU-II:



The Ekman Boundary Layer:  
Wind directions close to earth surface

### Project FAU-I:



Liquid propellant behavior under microgravity conditions

## International Cooperations

The network cooperates with international outstanding scientists:

- ▷ Prof. R. Eymard, Université de Marne-la-Vallée
- ▷ Prof. O. Knio, Johns-Hopkins-University, Bessel prize winner
- ▷ Prof. Ch. Schär, ETH Zürich, Institut für Atmosphäre und Klima